

1. **C** Set  $x$  and  $y$  components equal and solve for  $t$ .  $t = 4$  at  $(2, -3)$ ,  $t = 0$  at  $(0, 1)$ ,  $t = 1$  at  $(1, 0)$ , but  $-1 = \sqrt{t}$  has no solution, so the point not on the curve is  $(-1, 0)$ .

2. **D** 
$$\frac{\cos x}{1 + \sin x} \cdot \frac{(1 - \sin x)}{(1 - \sin x)} = \frac{\cos x(1 - \sin x)}{1 - \sin^2 x} = \frac{1 - \sin x}{\cos x} = \sec x - \tan x.$$

3. **A** Since  $-1 \leq \cos x \leq 1$ ,  $\frac{-1}{x} \leq \frac{\cos x}{x} \leq \frac{1}{x}$ . Since  $\pm \frac{1}{x} \rightarrow 0$  as  $x \rightarrow \infty$ , by the Squeeze Theorem, the limit is **0**.

4. **A** As we approach 4 from the right along the curve, the  $y$ -value approaches **4**.

5. **B** Let  $f(x) = x^3 - x^2 + x$ .  $f$  is continuous since it is a polynomial, and  $f(2) = 6$ ,  $f(3) = 21$ , so  $f(2) < 10 < f(3)$ . Therefore, by the **Intermediate Value Theorem**, there is a solution to  $f(x) = 10$  on  $[2, 3]$ .

6. **E**  $\mathbf{a} = (6\mathbf{i} + 3\mathbf{j}) - (-3\mathbf{i} + \mathbf{j}) = 9\mathbf{i} + 2\mathbf{j}$ . To form a unit vector  $\hat{\mathbf{a}}$ , multiply by the reciprocal of the magnitude:  $\hat{\mathbf{a}} = \frac{1}{\sqrt{9^2 + 2^2}}(9\mathbf{i} + 2\mathbf{j}) = \frac{9}{\sqrt{85}}\mathbf{i} + \frac{2}{\sqrt{85}}\mathbf{j}$ .

7. **B** 
$$\lim_{x \rightarrow 5^-} f(x) = 6 - 5 = 1.$$
 
$$\lim_{x \rightarrow 5^+} f(x) = -8 + 2(5) = 2,$$
 and  $f(5) = 1$ . Therefore, since  $\lim_{x \rightarrow 5^-} f(x) = f(5) \neq \lim_{x \rightarrow 5^+} f(x)$ ,  $f$  is **continuous only from the left**.

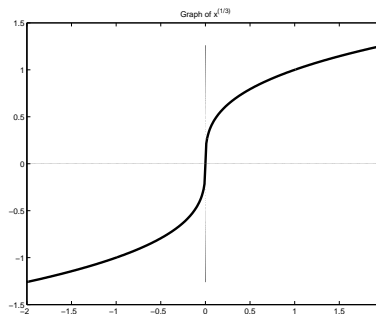
8. **E** Factor  $x$  from numerator and denominator: 
$$\lim_{x \rightarrow \infty} \frac{x(4 + \frac{9}{x})}{x(3 - \frac{8}{x})} = \frac{4}{3}.$$
 Similarly, 
$$\lim_{x \rightarrow -\infty} \frac{x(4 + \frac{9}{x})}{x(3 - \frac{8}{x})} = \frac{4}{3}.$$

9. **A** The angle between the gravity force (weight) and the motion of the block is  $30^\circ$ , so the work done is  $W = |\mathbf{F}||\mathbf{D}|\cos 30^\circ = (30)(20)\left(\frac{\sqrt{3}}{2}\right) = 300\sqrt{3}$  ft-lbs.

10. **B**  $f'(3) = \lim_{h \rightarrow 0} \frac{f(3+h) - f(3)}{h} = \lim_{h \rightarrow 0} h^2 - 4h + 7 = 7$ . The equation of the line whose slope is 7 and which passes through the point  $(3, 4)$  is  $y - 4 = 7(x - 3)$ , or  $\mathbf{y} = 7\mathbf{x} - 17$ .

11. **C**  $\lim_{x \rightarrow 3} \frac{x(x-3)}{x-3} = \lim_{x \rightarrow 3} x = 3$ .

12. **E** (a) is both continuous and differentiable everywhere; (c) and (d) are not continuous at  $x = 0$ . From the graph of (e), we see that the function continuous but not differentiable at  $x = 0$  is  $\sqrt[3]{x}$ .



13. 
$$f'(1) = \lim_{x \rightarrow 1} \frac{f(x) - f(1)}{x - 1} = \lim_{h \rightarrow 0} \frac{\sqrt{3+2x} - \sqrt{5}}{x - 1} \cdot \frac{\sqrt{3+2x} + \sqrt{5}}{\sqrt{3+2x} + \sqrt{5}}$$

$$= \lim_{x \rightarrow 1} \frac{3 + 2x - 5}{(x - 1)(\sqrt{3+2x} + \sqrt{5})}$$

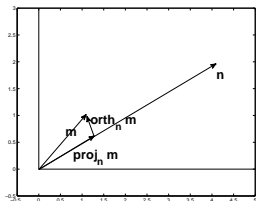
$$= \lim_{x \rightarrow 1} \frac{2(x - 1)}{(x - 1)(\sqrt{3+2x} + \sqrt{5})} = \lim_{x \rightarrow 1} \frac{2}{\sqrt{3+2x} + \sqrt{5}} = \frac{2}{2\sqrt{5}} = \frac{1}{\sqrt{5}}.$$

14. .
- (a)  $\text{proj}_{\mathbf{n}}\mathbf{m} = \frac{\mathbf{m} \cdot \mathbf{n}}{|\mathbf{n}|^2}\mathbf{n} = \frac{4 + 2}{(4^2 + 2^2)}\langle 4, 2 \rangle$   
 $= \left\langle \frac{6}{5}, \frac{3}{5} \right\rangle$ , so  $\text{orth}_{\mathbf{n}}\mathbf{m} = \langle 1, 1 \rangle - \left\langle \frac{6}{5}, \frac{3}{5} \right\rangle = \left\langle -\frac{1}{5}, \frac{2}{5} \right\rangle$ .

- (b) The point  $(0, 0)$  is on the line, so let  $\mathbf{b} = \langle 1, 1 \rangle - \langle 0, 0 \rangle = \langle 1, 1 \rangle$ . The vector  $\mathbf{v} = \langle 4, 2 \rangle$  is in the direction of the line, so  $\mathbf{v}^\perp = \langle -2, 4 \rangle$  is orthogonal to the line. The distance is found

$$\text{by } |\text{comp}_{\mathbf{v}^\perp} \mathbf{b}| = \frac{-2 + 4}{\sqrt{(-2)^2 + 4^2}} = \frac{2}{\sqrt{20}}$$

(NOTE that this is the magnitude of the vector in (a) above!)



15. Find a common denominator:

$$\begin{aligned} \lim_{x \rightarrow 2} \frac{\frac{1}{x} \cdot \frac{2}{2} - \frac{1}{2} \cdot \frac{x}{x}}{x-2} &= \lim_{x \rightarrow 2} \frac{1}{x-2} \cdot \frac{2-x}{2x} \\ &= \lim_{x \rightarrow 2} -\frac{1}{2x} = -\frac{1}{4}. \end{aligned}$$

16.  $\mathbf{F}_1 = \langle 8 \cos 45^\circ, 8 \sin 45^\circ \rangle = \langle 4\sqrt{2}, 4\sqrt{2} \rangle$ .  
 $\mathbf{F}_2 = \langle 14 \cos 60^\circ, -14 \sin 60^\circ \rangle = \langle 7, -7\sqrt{3} \rangle$ .  
 The resultant force is  $\mathbf{F}_1 + \mathbf{F}_2 = \langle 4\sqrt{2} + 7, 4\sqrt{2} - 7\sqrt{3} \rangle$ . Therefore, the magnitude of the resultant force is  $\sqrt{(4\sqrt{2} + 7)^2 + (4\sqrt{2} - 7\sqrt{3})^2}$ .

17. We use  $\mathbf{r}(t) = \mathbf{r}_0 + t\mathbf{v}$  to find the parametric equations.  $\mathbf{r}_0$  corresponds to the point at  $t = 1$  :  $\mathbf{r}(1) = 5\mathbf{i} + 5\mathbf{j}$ .  $\mathbf{v} = \mathbf{r}'(1) = \lim_{t \rightarrow 1} \frac{((5t)\mathbf{i} + (8 - 3t^2)\mathbf{j}) - (5\mathbf{i} + 5\mathbf{j})}{t-1} = \lim_{t \rightarrow 1} \frac{(5t-5)\mathbf{i} + (3-3t^2)\mathbf{j}}{t-1} = \lim_{t \rightarrow 1} \left( \frac{5t-5}{t-1} \right) \mathbf{i} + \left( \frac{3-3t^2}{t-1} \right) \mathbf{j} = \left( \lim_{t \rightarrow 1} \frac{5(t-1)}{t-1} \right) \mathbf{i} + \left( \lim_{t \rightarrow 1} \frac{3(1+t)(1-t)}{t-1} \right) \mathbf{j} = 5\mathbf{i} - 6\mathbf{j}$ . Therefore, the vector equation of the tangent line is  $\mathbf{r}(t) = (5\mathbf{i} + 5\mathbf{j}) + t(5\mathbf{i} - 6\mathbf{j})$ , so the parametric equations are  $\mathbf{r}(t) = (5 + 5t)\mathbf{i} + (5 - 6t)\mathbf{j}$ , or  $\mathbf{x} = 5 + 5t$ ,  $\mathbf{y} = 5 - 6t$ .